

$$T_{b \rightarrow a} = \begin{pmatrix} \sqrt{12} & -2\sqrt{12} & \sqrt{12} & 0 \\ 0 & \sqrt{12} & 3\sqrt{12} & 0 \\ 0 & 0 & \sqrt{12} & 0 \\ 0 & 0 & 0 & \sqrt{12} \end{pmatrix}$$

$$T_{a \rightarrow b} = \frac{1}{\sqrt{12}} \begin{pmatrix} 1 & 2 & -1 & 0 \\ 0 & 1 & -3 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$T_{A \rightarrow B} = A^{-1} \cdot B$$

$$(T_{A \rightarrow B})^{-1} = (A^{-1} \cdot B)^{-1} = B^{-1} \cdot A = T_{B \rightarrow A}$$

$$3) X' = (T_{B \rightarrow B'})^{-1} \cdot X$$

$$X' = T_{B' \rightarrow B} \cdot X$$

$$p' = T_{b \rightarrow a} \cdot p$$

$$p' = \begin{pmatrix} 1 & -2 & 1 & 0 \\ 0 & 1 & 3 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} -8 \\ -4 \\ 2 \\ 0 \end{pmatrix} \cdot \sqrt{12} = \begin{pmatrix} 2 \\ 2 \\ 2 \\ 0 \end{pmatrix} \cdot \sqrt{12}$$

$$q' = T_{b \rightarrow a} \cdot q$$

$$q' = \begin{pmatrix} 1 & -2 & 1 & 0 \\ 0 & 1 & 3 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} -12 \\ -8 \\ 3 \\ 1 \end{pmatrix} \cdot \sqrt{12} = \begin{pmatrix} 1 \\ 3 \\ 1 \\ 1 \end{pmatrix} \cdot \sqrt{12}$$